

NRES_798_9_201501

Linear model
applications

Fixed vs. Random factors

- Two different types of categorical explanatory variables
- Fixed
 - Treatment levels are the only ones of interest
 - Inference restricted to the treatment levels
 - Treatment contains constant information that is universal across populations (e.g. sex)
 - Set or selected by researcher
- Random
 - Treatment levels are a random sample of all possible levels
 - Inferences intended to extend beyond treatment levels tested
 - Treatments are not constrained and constant across populations (e.g. genotype)
 - Set by drawing samples from a broader underlying distribution

Fixed vs. Random effects

- Drug administered or not
- Block within a field
- Insecticide sprayed
- Brood
- Nutrients added
- One country vs. another
- History of development
- Split plot within a plot
- Family
- Untreated individuals
- Parent
- Light vs. shade
- One age vs. another

Fixed vs. Random effects (blue fixed)

- Drug administered or not
- Block within a field
- Insecticide sprayed
- Brood
- Nutrients added
- One country vs. another
- History of development
- Split plot within a plot
- Family
- Untreated individuals
- Parent
- Light vs. shade
- One age vs. another

Fixed vs. Random factor

- Mean square values and F-ratio structure differ between fixed and random factors
 - Only applicable to two-way ANOVA
- Fixed factor
 - F-ratio: main effects and interactions are compared against the residual mean square

$$F - ratio_A = \frac{\text{explained variance}}{\text{unexplained variance}} = \frac{MS_A}{MS_{\text{within groups}}}$$

$$F - ratio_{AB} = \frac{\text{explained variance}}{\text{unexplained variance}} = \frac{MS_{AB}}{MS_{\text{within groups}}}$$

- Focus on increasing replication within treatments
 - i.e. inference focuses on treatments therefore replicates increase power

Fixed vs. Random factor

- Random factor
 - F-ratio: main effects are tested against the interaction mean square, interaction effect tested against within group mean square

$$F - ratio_A = \frac{\text{explained variance}}{\text{unexplained variance}} = \frac{MS_A}{MS_{AB}}$$

$$F - ratio_{AB} = \frac{\text{explained variance}}{\text{unexplained variance}} = \frac{MS_{AB}}{MS_{\text{within groups}}}$$

- Focus on increasing the number of treatment levels established
 - i.e. inference focuses on sampling distribution therefore more treatment levels increase power
 - When to give up on ANOVA and use regression?
- Random block and repeated measures analysed as random factors

Two-way ANOVA



ANIMAL BEHAVIOUR, 2000, 60, 511–521
doi:10.1006/anbe.2000.1513, available online at <http://www.idealibrary.com> on IDEAL®



Lack of preference for low-predation-risk habitats in larval damselflies explained by costs of intraspecific interactions

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(Received 16 August 1998; initial acceptance 28 September 1999;
final acceptance 26 April 2000; MS. number: A8566)

Many studies indicate prey organisms select microhabitats with high structural complexity as a way of reducing risk of predation. We used laboratory experiments to show that damselfly larvae, *Ischnura verticalis*, suffer higher predation rates from pumpkinseed sunfish in low-density vegetation. However, larvae do not preferentially occupy microhabitats with high vegetation density in either the presence or absence of sunfish; when given a choice, the number of larvae per stem of vegetation was equal across all densities of vegetation. That larvae do not congregate in dense vegetation may reflect costs of aggressive interactions. Results from laboratory experiments indicated larval interactions increase conspicuous behaviours (most notably swimming) and consequently increase fish predation. A subsequent experiment indicated that frequency of larval interactions increases with increased vegetation density when number of larvae/stem is constant. Thus, larval microhabitat selection may reflect a trade-off between reduced risk of predation in areas of high vegetation density, caused by reduced fish foraging ability, and increased aggressive larval interactions, due to decreased proximity of larvae.

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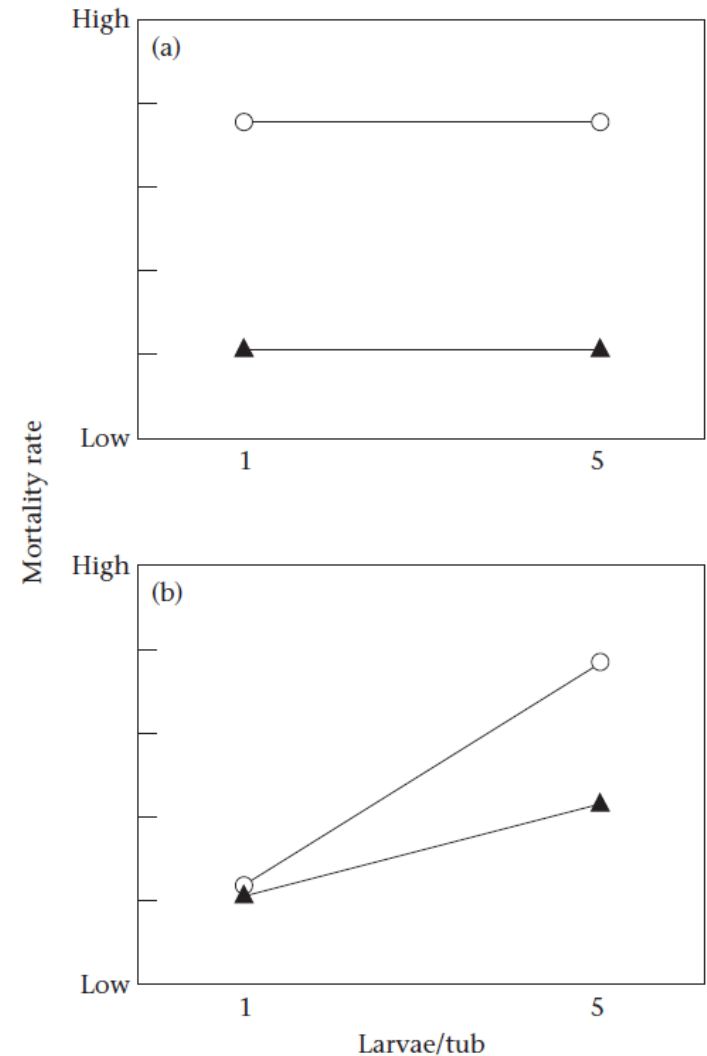


Figure 3. Scenarios of possible mortality rates. (a) Expected mortality due to an increase in the ability of fish to detect larvae, independent of larval interactions. (b) Expected mortality as positively related to frequency of larval interactions. (○: low vegetation; ▲: high vegetation) See text for details.

Two-way ANOVA

- Vegetation density ($p = 0.0002$)
- Conspecifics ($p = 0.0026$)
- Interaction ($p = 0.1589$)
- $\text{Log}_{10}(X + 1)$ transformed

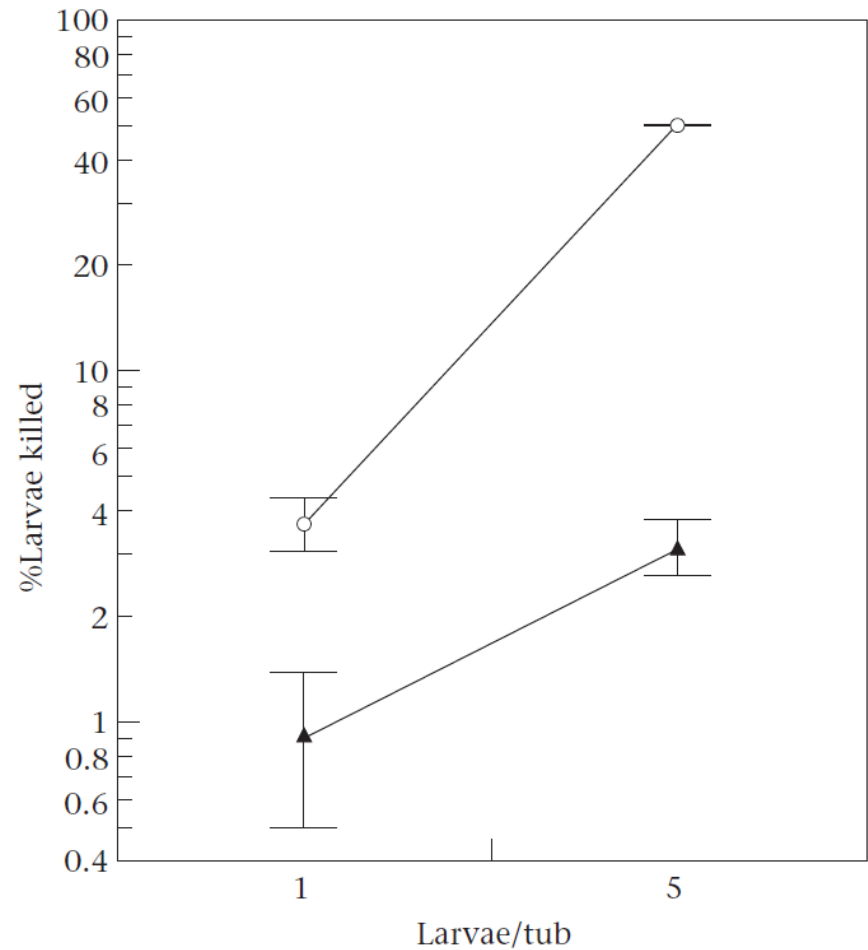
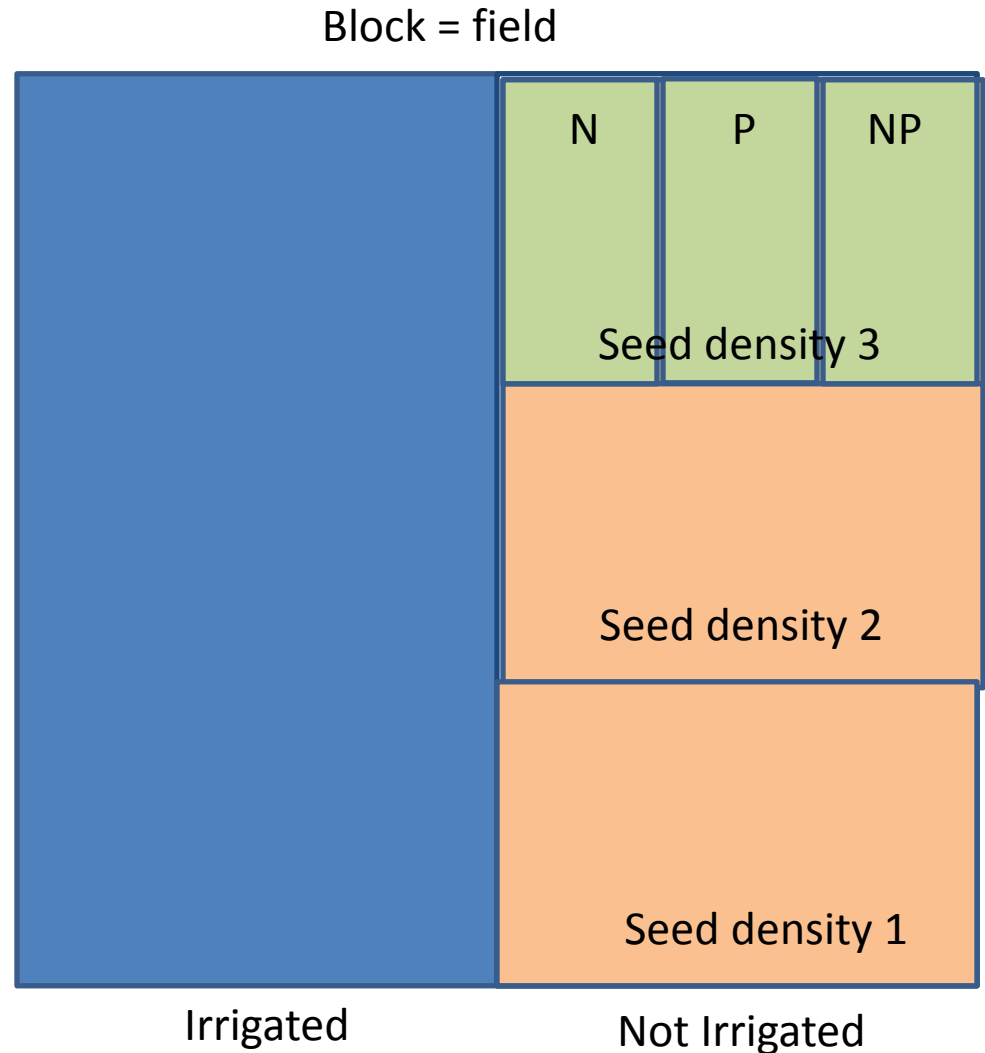


Figure 4. Mean \pm SE percentage of larvae killed under various conditions of larvae (one versus five per tub) and vegetation density. (○: low vegetation; ▲: high vegetation) Values presented are back transformed.

Split plot ANOVA

- Experiment examining the influence of irrigation, seed density and fertilization on crop yield
- Blocks: 4 fields
- Irrigation: 2 levels
- Seeding density: 3 levels
- Fertilization: 3 levels



Split plot ANOVA

```
> str(yields)
```

```
'data.frame':      72 obs. of  5 variables:
```

```
$ yield   : int  90 95 107 92 89 92 81 92 93 80 ...
```

```
$ block   : Factor w/ 4 levels "A","B","C","D": 1 1 1 1 1 1 1 1 1 1 ...
```

```
$ irrigation: Factor w/ 2 levels "control","irrigated": 1 1 1 1 1 1 1 1 1 2 ...
```

```
$ density   : Factor w/ 3 levels "high","low","medium": 2 2 2 3 3 3 1 1 1 2 ...
```

```
$ fertilizer: Factor w/ 3 levels "N","NP","P": 1 3 2 1 3 2 1 3 2 1 ...
```

```
> yields
```

```
yield block irrigation density fertilizer
```

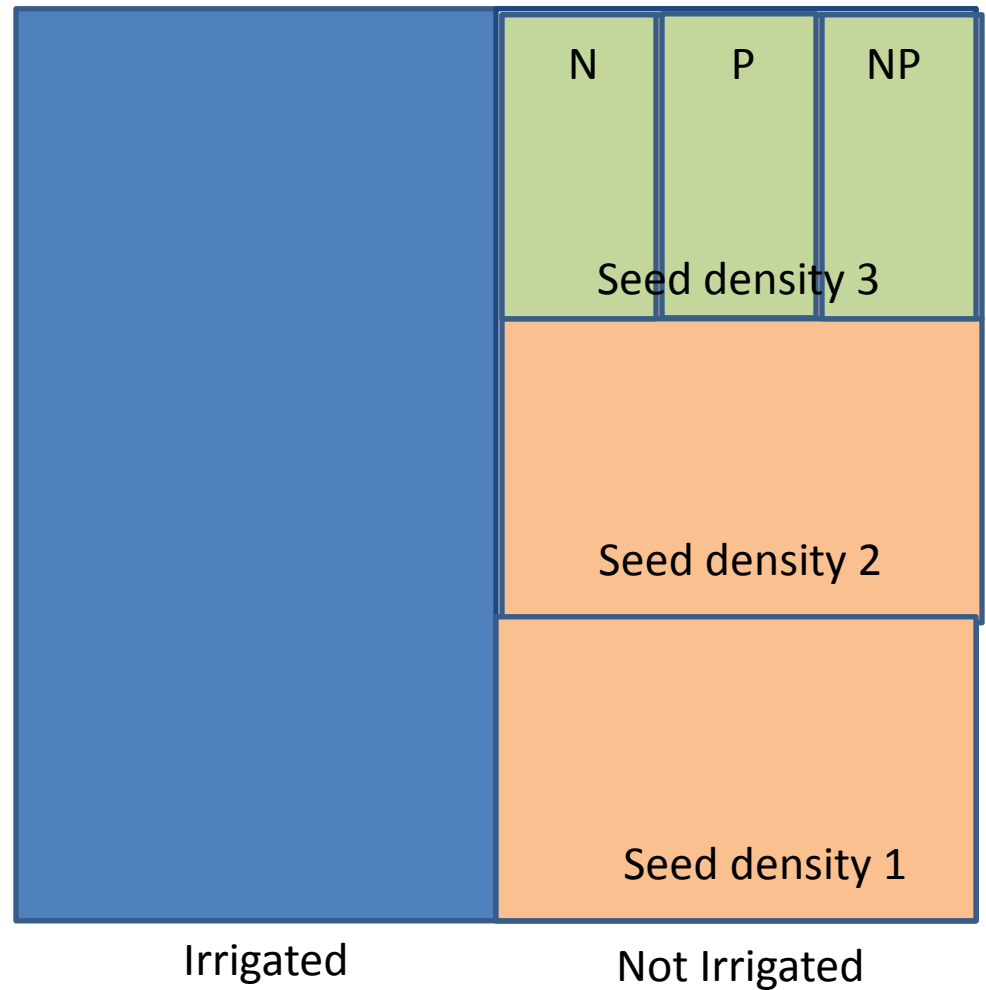
1	90	A	control	low	N
2	95	A	control	low	P
3	107	A	control	low	NP
4	92	A	control	medium	N
5	89	A	control	medium	P
6	92	A	control	medium	NP
7	81	A	control	high	N
8	92	A	control	high	P
9	93	A	control	high	NP
10	80	A	irrigated	low	N
11	87	A	irrigated	low	P

$$4 * 2 * 3 * 2 = 72$$

Split plot ANOVA

```
model_bad <- aov(yield~irrigation*density*fertilizer)
summary(model_bad)
```

Block = field



Split plot ANOVA

```
model_bad <- aov(yield~irrigation*density*fertilizer)
summary(model_bad)
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
irrigation	1	8278	8278	59.575	2.81e-10	***
density	2	1758	879	6.328	0.00340	**
fertilizer	2	1977	989	7.116	0.00181	**
irrigation:density	2	2747	1374	9.885	0.00022	***
irrigation:fertilizer	2	953	477	3.431	0.03956	*
density:fertilizer	4	305	76	0.549	0.70082	
irrigation:density:fertilizer	4	235	59	0.422	0.79183	
Residuals	54	7503	139			

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Split plot ANOVA

```
model <- aov(yield ~ irrigation*density*fertilizer + Error(block/irrigation/density))
summary(model)
```

Four ANOVA tables one for each plot size

Error: block

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Residuals	3	194.4	64.81		

Error: block:irrigation

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
irrigation	1	8278	8278	17.59	0.0247 *
Residuals	3	1412	471		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Error: block:irrigation:density

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
density	2	1758	879.2	3.784	0.0532 .
irrigation:density	2	2747	1373.5	5.912	0.0163 *
Residuals	12	2788	232.3		

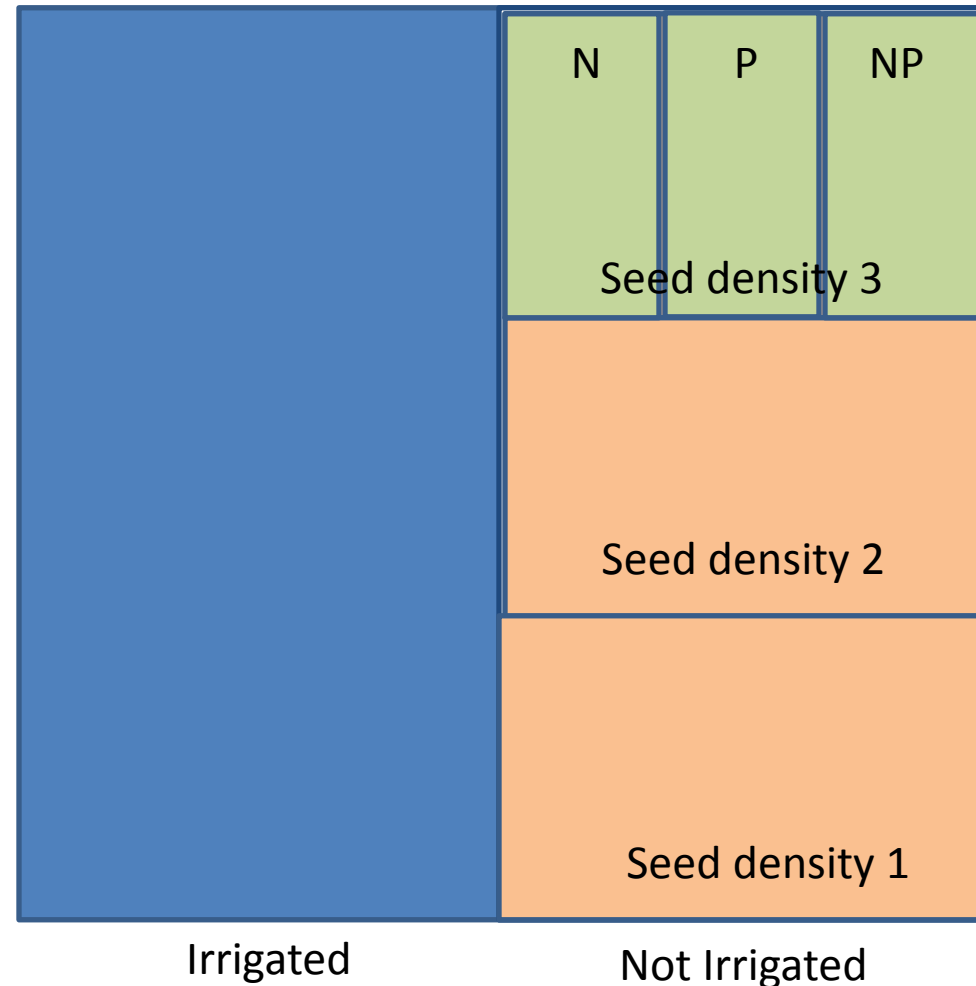
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Error: Within

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
fertilizer	2	1977.4	988.7	11.449	0.000142 ***
irrigation:fertilizer	2	953.4	476.7	5.520	0.008108 **
density:fertilizer	4	304.9	76.2	0.883	0.484053
irrigation:density:fertilizer	4	234.7	58.7	0.680	0.610667
Residuals	36	3108.8	86.4		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Block = field



Split plot ANOVA

```
model <- aov(yield ~ irrigation*density*fertilizer + Error(block/irrigation/density))
summary(model)
```

```
Error: block
      Df Sum Sq Mean Sq F value Pr(>F)
Residuals 3  194.4   64.81

Error: block:irrigation
      Df Sum Sq Mean Sq F value Pr(>F)
irrigation 1  8278   8278  17.59 0.0247 *
Residuals  3  1412    471

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Error: block:irrigation:density
      Df Sum Sq Mean Sq F value Pr(>F)
density 2  1758   879.2   3.784 0.0532 .
irrigation:density 2  2747  1373.5  5.912 0.0163 *
Residuals  12  2788   232.3

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

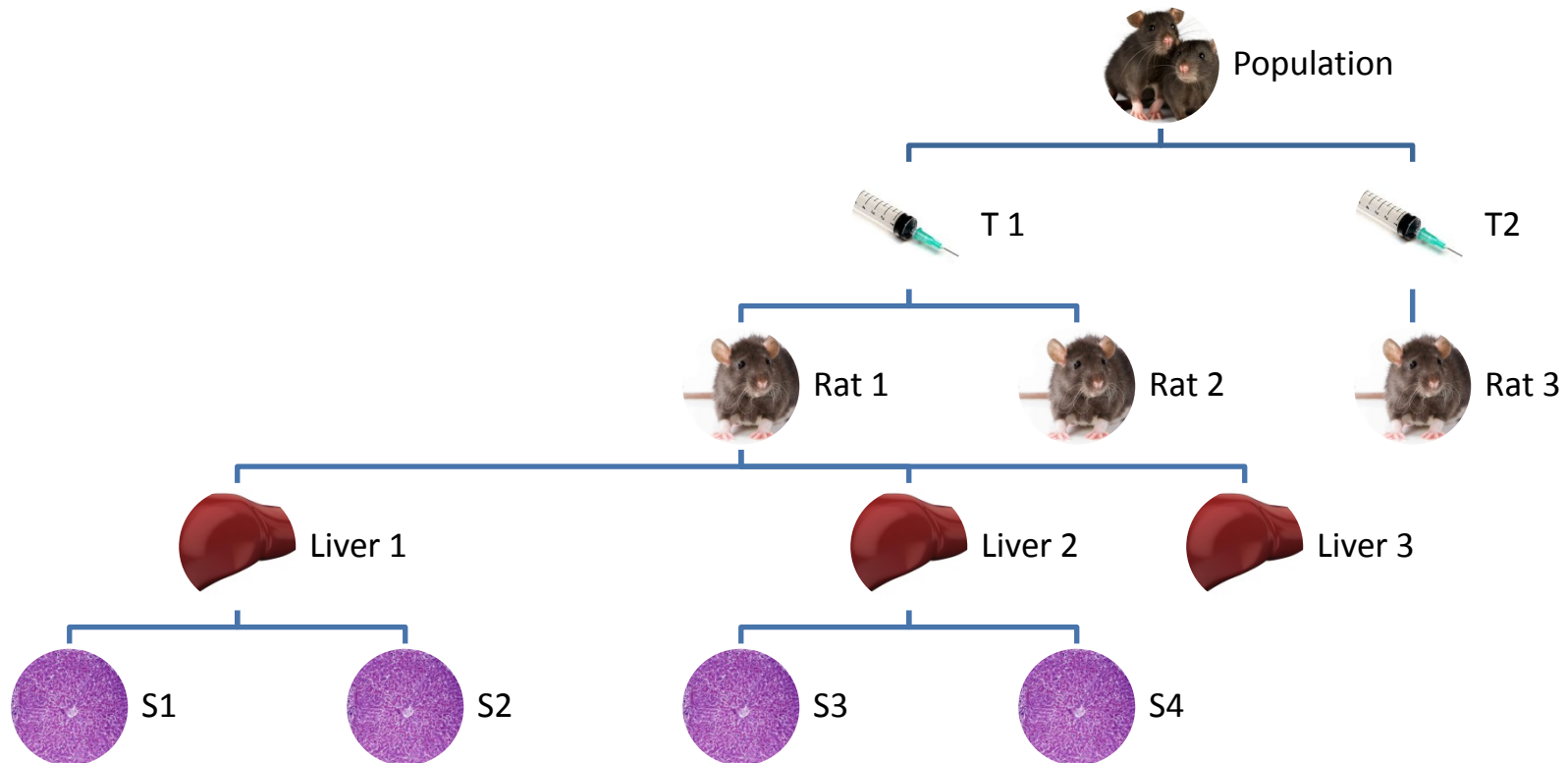
Error: Within
      Df Sum Sq Mean Sq F value Pr(>F)
fertilizer 2  1977.4  988.7  11.449 0.000142 ***
irrigation:fertilizer 2  953.4  476.7   5.520 0.008108 **
density:fertilizer 4  304.9   76.2   0.883 0.484053
irrigation:density:fertilizer 4  234.7   58.7   0.680 0.610667
Residuals 36  3108.8   86.4

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Nested ANOVA

- Influence of treatment on rat liver Glycogen content

3 treatments (T1, T2, T3)
2 rats/treatment
3 liver sections
2 preparations of each liver section



Nested ANOVA

```
datpath <- "C:/Users/Che/UNBC_work/Courses/NRES-798/NRES-798-Labs/therbook/rats.txt"
rats <- read.table(datpath,header=TRUE)
attach(rats)
names(rats)
str(rats)
```

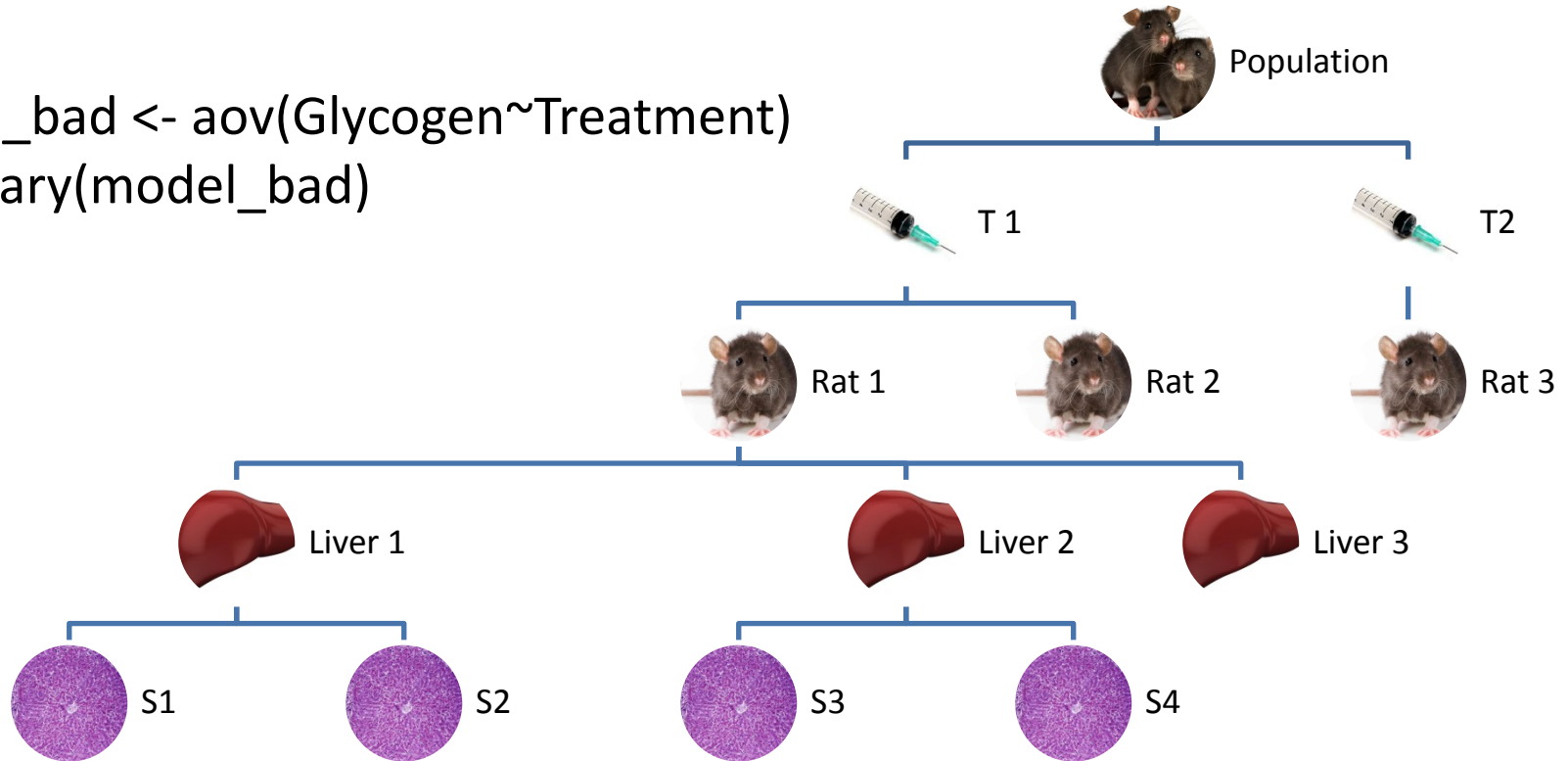
```
Treatment<-factor(Treatment)
Rat<-factor(Rat)
Liver<-factor(Liver)
```

```
> str(rats)
'data.frame':      36 obs. of  4 variables:
 $ Glycogen : int  131 130 131 125 136 142 150
148 140 143 ...
 $ Treatment: int  1 1 1 1 1 1 1 1 1 1 ...
 $ Rat      : int  1 1 1 1 1 1 2 2 2 2 ...
 $ Liver    : int  1 1 2 2 3 3 1 1 2 2 ...
```

	Glycogen	Treatment	Rat	Liver
1	131	1	1	1
2	130	1	1	1
3	131	1	1	2
4	125	1	1	2
5	136	1	1	3
6	142	1	1	3
7	150	1	2	1
8	148	1	2	1

Nested ANOVA

```
model_bad <- aov(Glycogen~Treatment)
summary(model_bad)
```



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Treatment	1	170.7	170.67	1.837	0.184
Residuals	34	3159.6	92.93		

Pseudo replication
 $3*2*3*2 = 36$

Nested ANOVA

```
model <- aov(Glycogen ~ Treatment + Error(Treatment/Rat/Liver))
summary(model)
```

Error: Treatment

	Df	Sum Sq	Mean Sq
Treatment	1	170.7	170.7

Error: Treatment:Rat

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Residuals	1	148.6	148.6		

Error: Treatment:Rat:Liver

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Residuals	1	0.03214	0.03214		

Error: Within

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Residuals	32	3011	94.09		

$$SS_{among\ groups} = \sum_{i=1}^a \sum_{j=1}^b \sum_{k=1}^n (\bar{Y}_i - \bar{Y})^2$$

$$SS_{replicates(groups)} = \sum_{i=1}^a \sum_{j=1}^b \sum_{k=1}^n (\bar{Y}_{j(i)} - \bar{Y}_i)^2$$

$$SS_{subsamples} = \sum_{i=1}^a \sum_{j=1}^b \sum_{k=1}^n (Y_{ijk} - \bar{Y}_{j(i)})^2$$

The correction factor at any level is the uncorrected sum of squares from the level above

Nested ANOVA vs. Split plot ANOVA

- Nested ANOVA: uninformative factor levels
 - E.g. rat, liver bit, liver preparation
- Split plot ANOVA: informative factor levels
 - E.g. seed density, fertilizer, irrigation

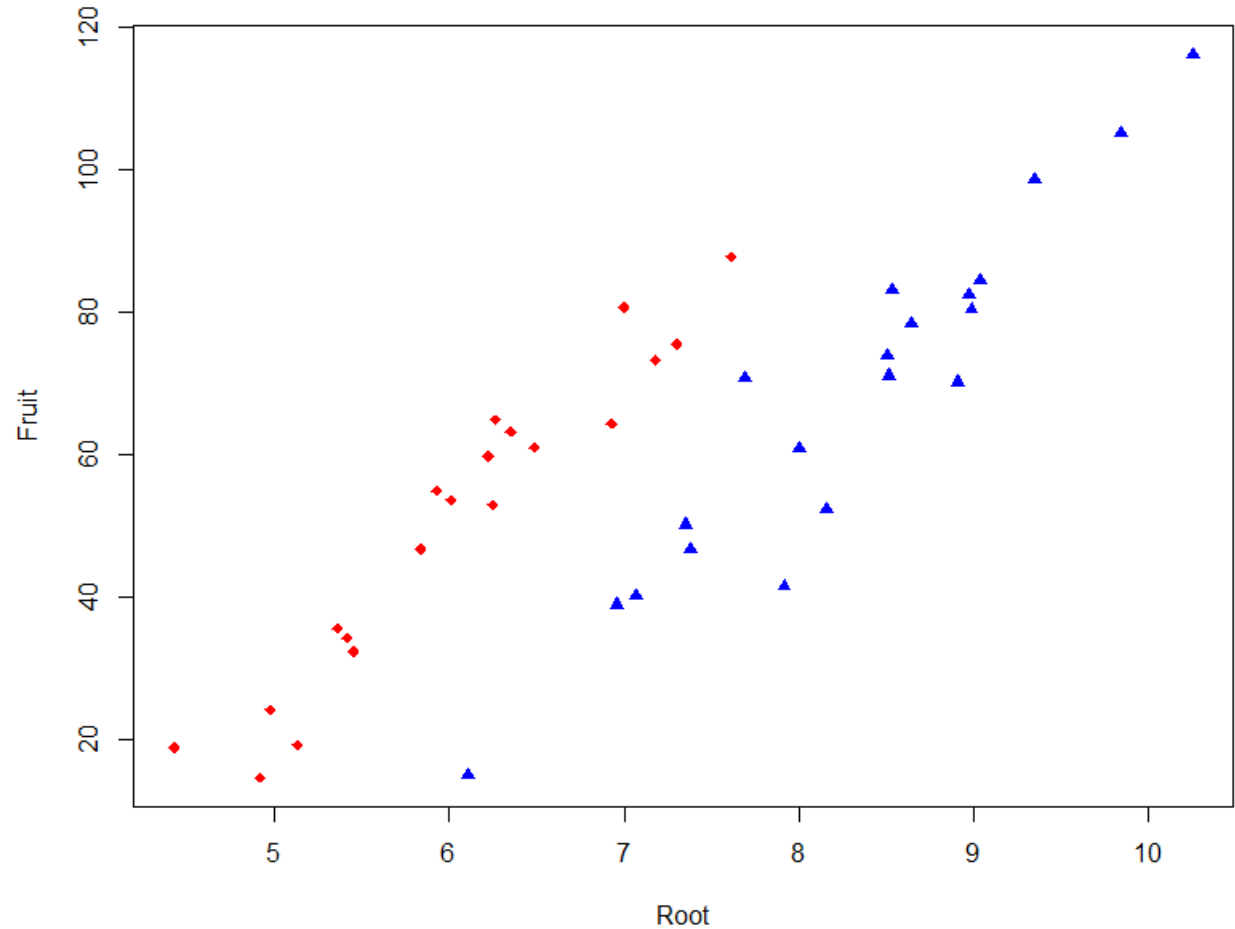
ANCOVA

- Impact of grazing on seed production of a biennial plant
- 2 treatments: grazed, ungrazed
- Diameter of rootstock measured
- Mass of fruit measured
- 40 individuals total



Ipomopsis rubra

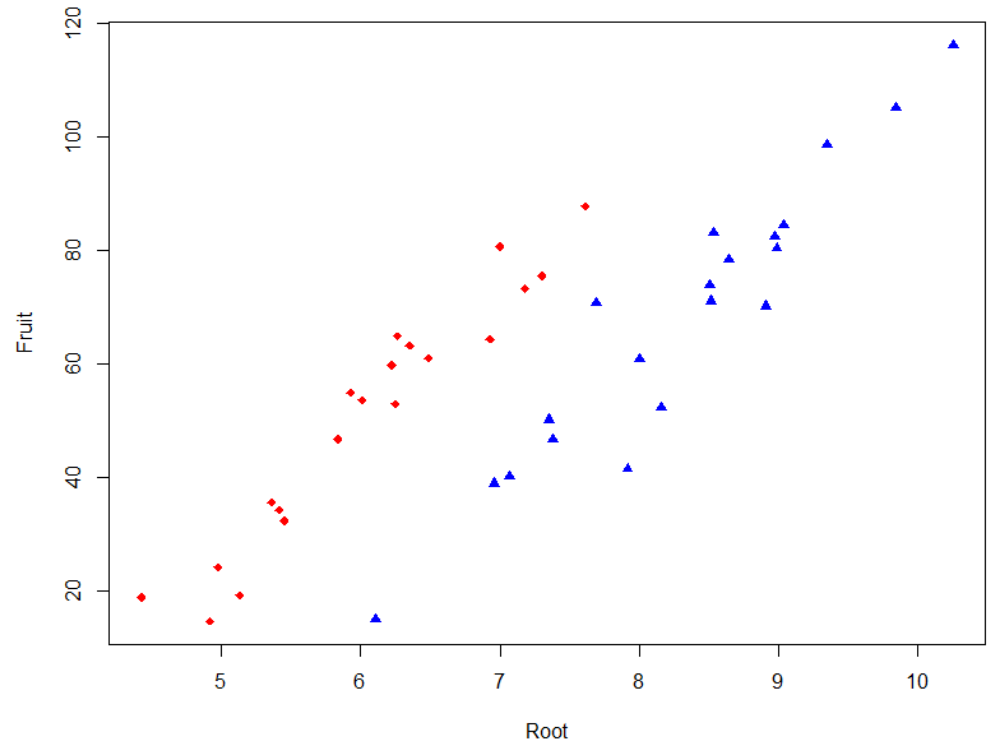
ANCOVA



- Red grazed
- Blue Ungrazed

ANCOVA

- Red grazed
- Blue Ungrazed



- Fit complex model first
- `ancova <- lm(Fruit~Grazing*Root)`
- `summary(ancova)`

ANCOVA

Call:

`lm(formula = Fruit ~ Grazing * Root)`

Residuals:

Min	1Q	Median	3Q	Max
-17.3177	-2.8320	0.1247	3.8511	17.1313

Coefficients:

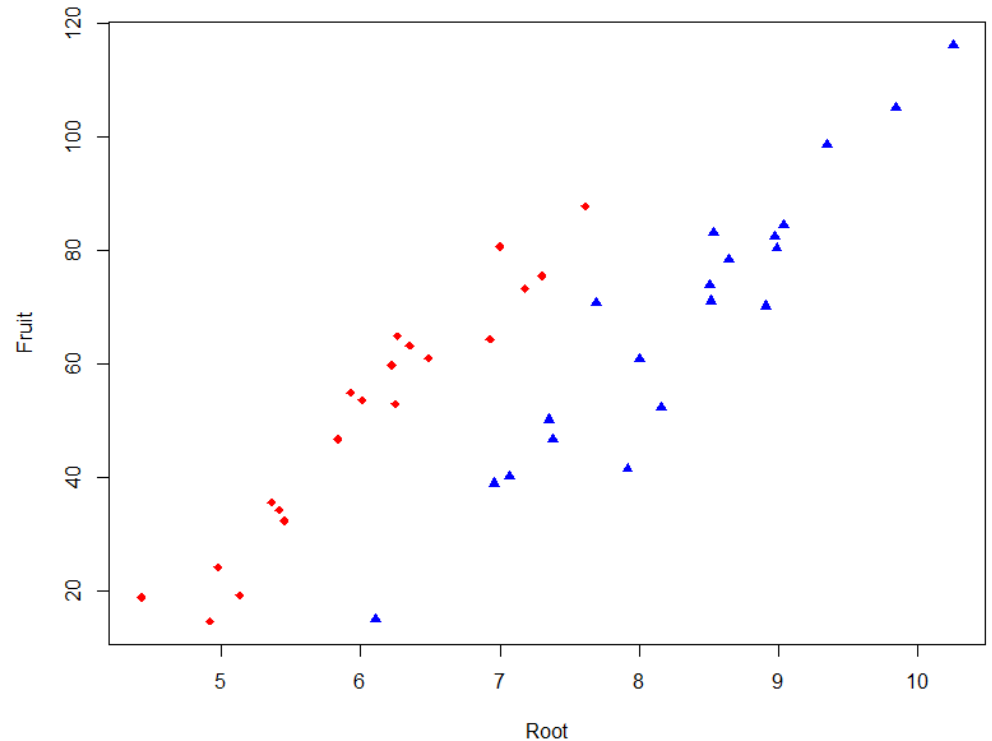
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-125.173	12.811	-9.771	1.15e-11 ***
GrazingUngrazed	30.806	16.842	1.829	0.0757 .
Root	23.240	1.531	15.182	< 2e-16 ***
GrazingUngrazed:Root	0.756	2.354	0.321	0.7500

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

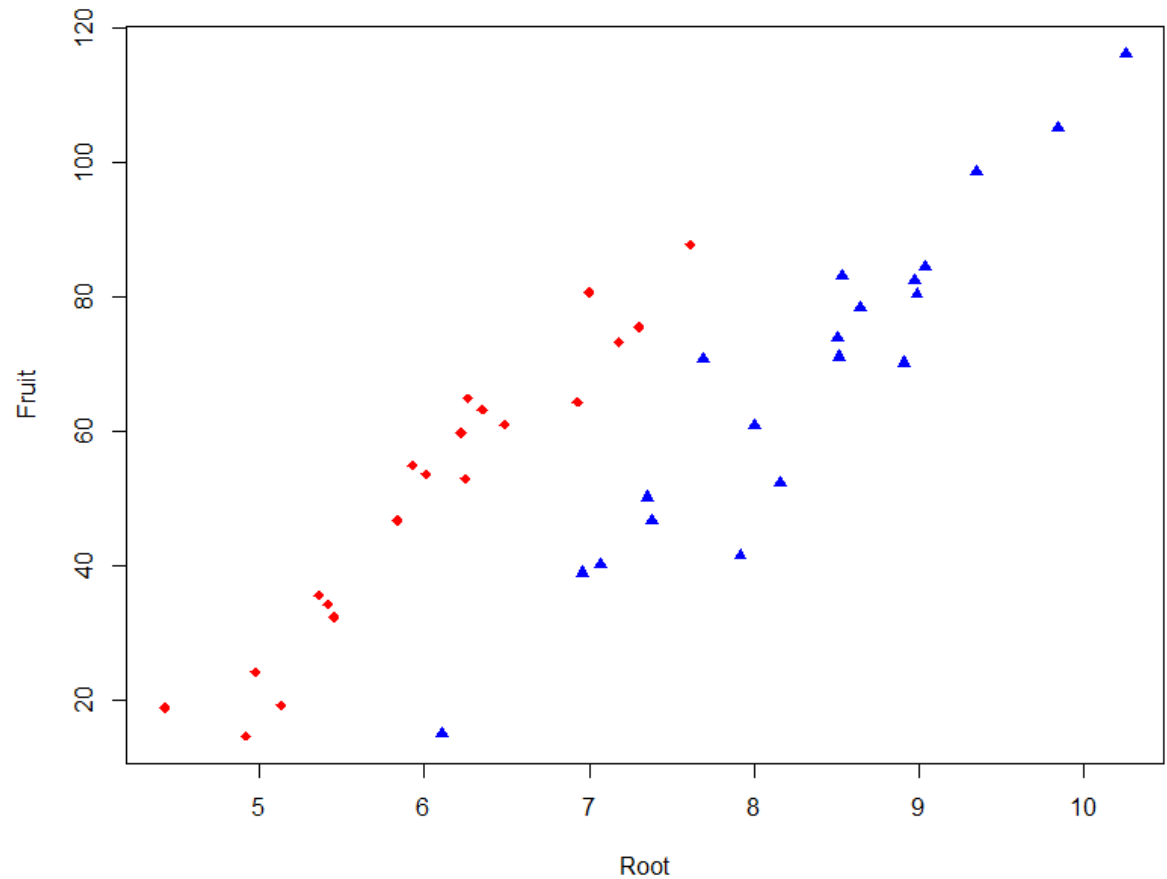
Residual standard error: 6.831 on 36 degrees of freedom

Multiple R-squared: 0.9293, Adjusted R-squared: 0.9234

F-statistic: 157.6 on 3 and 36 DF, p-value: < 2.2e-16



ANCOVA



Analysis of Variance Table

Response: Fruit

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Grazing	1	2910.4	2910.4	62.3795	2.262e-09 ***
Root	1	19148.9	19148.9	410.4201	< 2.2e-16 ***
Grazing:Root	1	4.8	4.8	0.1031	0.75
Residuals	36	1679.6	46.7		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1