# BIOL 410 Population and Community Ecology 

Population sampling<br>Calculating vital rates

## Population sampling strategies

- Random sampling


Number
Density

- Stratified random sampling
- Stratified sampling
- Systematic sampling
- Objective: high accuracy, least bias, greatest precision, lowest cost



## Sampling and population estimates



- Mean

$$
\bar{X}=\frac{\sum X_{i}}{n}
$$

- Population, subpopulation, strata


## Sampling and population estimates



- Mean

$$
\bar{X}=\frac{\sum X_{i}}{n}
$$

- Variance

$$
s^{2}=\frac{\sum\left(X_{i}-\bar{X}\right)^{2}}{n-1}
$$

## Sampling and population estimates



- Standard deviation
- Confidence intervals (95\% confidence intervals)

$$
s=\sqrt{s^{2}}=\sqrt{\frac{\sum\left(X_{i}-\bar{X}\right)^{2}}{n-1}}
$$



$$
\begin{aligned}
& \text { lower } C I=\bar{X}+1.96 \frac{s}{\sqrt{n}} \\
& \text { upper } C I=\bar{X}+1.96 \frac{s}{\sqrt{n}}
\end{aligned}
$$

## Confidence intervals



Upper $C I=\bar{X}+1.96 \frac{s}{\sqrt{n}}$

```
N <- rnorm(500,80,15)
upper <- rep(NA,length(N))
lower <- rep(NA,length(N))
nhold <- rep(NA,length(N))
shold <- rep(NA,length(N))
for(i in 1:length(N)){
    Nsample <- sample(N,i,replace = FALSE)
    n <- mean(Nsample[1:i])
    s <- sd(Nsample[1:i])
    nhold[i] <- mean(Nsample[1:i])
    shold[i] <- sd(Nsample[1:i])
    error <- qnorm(0.975)*s/sqrt(n)
    upper[i]<- n + error
    lower[i] <- n - error
}
i <- c(1:length(N))
jpeg("confidence_interval.jpg")
par(cex=1.5)
plot(i,nhold,ylim=c(68,92),ylab="mean",xl
ab="# samples",pch=16)
points(i,upper,type="l",col="red")
points(i,lower,type="l",col="blue")
points(i,nhold,col="black",pch=16)
dev.off()
```


## Sampling and population estimates



- Accuracy: correct mean
- Precision: small variance, small 95\% confidence intervals
- Bias: least bias possible

$$
s=\sqrt{s^{2}}=\sqrt{\frac{\sum\left(X_{i}-\bar{X}\right)^{2}}{n-1}}
$$

## Ecological sampling methods



UBC
https://www.zoology.ubc.ca/~krebs/ecological_rants/


## Quadrat counts

- Count plants/ animals in a known area
- Simplest technique fore density estimation
- Counts can be taken from units using any number of sample designs: random, stratified random, systematic..

- Assumptions
- All individuals in the quadrate are observed
- Quadrat samples are representative of the study area as a whole
- Individuals don't move between quadrats during a sampling session



## Use of quadrat counts

- Spatial considerations
- Edge to area ratio: circle < square < rectangle
- Edge can result in arbitrary decisions about inclusion, but difficult to traverse round edge
- Shape dependent on sampling problem
- Size
- Balance sample variance with cost of placeman and collection
- Total cost $=$ fixed costs + sampling costs
- Minimize (Total costs)*(Observed Variance)


## Optimized quadrat counts

- Wiegert's Method
- Quadrat size that minimizes relative cost and relative variability

|  | Quadrat size (area) |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 3 | 4 | 12 | 16 |
| Fixed cost (\$) | 10 | 10 | 10 | 10 | 10 |
| Cost per sample (\$) | 2 | 6 | 8 | 24 | 32 |
| Total cost for one quadrat (\$) | 12 | 16 | 18 | 34 | 42 |
| Relative cost for one quadrat | 1 | 1.33 | 1.50 | 2.83 | 3.50 |

We need to balance these costs against the relative variability of samples taken with quadrats of different sizes:

|  | Quadrat size (area) |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 3 | 4 | 12 | 16 |
| Observed variance per $0.25 \mathrm{~m}^{2}$ | 0.97 | 0.24 | 0.32 | 0.14 | 0.15 |

## Optimized quadrat counts

- Wiegert's Method
- Quadrat size that minimizes relative cost and relative variability



## Quadrat counts

- Calculating abundance
- Total/Minimum count
- Restrict estimate to statistical population
- Limited inference
- Simple density estimate
- Extrapolate estimate (n/m2) to uncounted units and/or biological population
- Best to stratify
- Statistical extrapolation
- Relate distribution of counts to a statistical distribution
- Use count distribution not continuous distribution
- Devise statistical "model" that estimates/explains populations


## Quadrat counts

- Simple density estimates
- (areal survey)
- Equal size sample units
- Randomly sample n quadrates from N quadrats in statistical population
- Mean number of animals per quadrat: $\quad \bar{x}=\frac{\sum x}{n}$
- Total number:

$$
\hat{x}=N \bar{x}
$$

- Variance of sample

$$
\begin{aligned}
& \hat{s}^{2}=\frac{\sum x^{2}-\left(\sum x\right)^{2} / n}{n-1} \\
& \left(N s_{\bar{x}}\right)^{2}=\frac{N^{2}}{n} s^{2}\left(1-\frac{n}{N}\right)
\end{aligned}
$$

- Variance of estimate

Sampling without replacement

## Quadrat counts

- Statistical extrapolation
- Relate distribution of counts to a statistical distribution
- Use count distribution not a continuous distribution
- Devise a statistical model that estimates population size



## Line transects

- Used to calculate density of animals in rectangular "quadrats"



## Line transects

- Used to calculate density of animals in rectangular "quadrats"
- If detectability $100 \%$ simple count
- If detectability $<100 \%$ then develop detection function to estimate density

$$
\widehat{D}=\frac{n}{2 L a}
$$

```
\(\widehat{D}=\) density of animals per unit area
\(\mathrm{n}=\) number of animals seen on transect
\(\mathrm{L}=\) length of transect
a = detection constant (detection probability vs distance)
```


## Estimators of detection distance (a)

- Hayne’s estimator

- Assumes fixed flushing distance correction for (a)

$$
\hat{D}_{H}=\frac{n}{2 L}\left(\frac{1}{n} \sum 1 / r_{i}\right)
$$

where $\hat{D}_{H}=$ Hayne's estimator of density

$$
\begin{aligned}
& n=\text { number of animals seen } \\
& L=\text { length of transect } \\
& r_{i}=\text { sighting distance to each animal } i
\end{aligned}
$$

## Estimators of detection distance (a)

- Hayne's estimator

- Variance of Hayne's density estimate

$$
\operatorname{Var}\left(\hat{D}_{H}\right)=D_{H}^{2}\left[\frac{\operatorname{var}(\mathrm{n})}{\mathrm{n}^{2}}+\frac{\sum\left(1 / r_{i}-R\right)^{2}}{R^{2} n(n-1)}\right]
$$

where $\hat{D}_{H}=$ Hayne's estimator of density

$$
n=\text { number of animals seen }
$$

$$
\operatorname{var}(n)=\text { variance of } n \cong n
$$

$$
r_{i}=\text { sighting distance for animal } i
$$

$R=$ mean of the reciprocals of sighting distances $i$

## Distance methods

- Distance of a random point to the nearest organism
- Distance of a random organism to its nearest neighbour



## Distance methods

- T-square sampling procedure
- Distance from random point to nearest organism
- Distance from the organism to its nearest neighbour



## Distance methods

- T-square sampling procedure


where $\quad \hat{N}_{1}=$ Estimate of population density from point-to-organism data $n=$ Sample size $x_{i}=$ Distance from random point $i$ to nearest organism


## Distance methods

- T-square sampling procedure

$$
\hat{N}_{1}=\frac{n}{\pi \sum\left(x_{i}^{2}\right)}
$$

where $\hat{N}_{1}=$ Estimate of population density from point-to-organism data $n=$ Sample size $x_{i}=$ Distance from random point $i$ to nearest organism

$$
\hat{N}_{2}=\frac{2 n}{\pi \sum\left(z_{i}^{2}\right)}
$$



## Distance methods

- T-square sampling procedure
- Compound measure using $\mathrm{N}_{1}, \mathrm{~N}_{2}$

$$
\hat{N}_{T}=\frac{n^{2}}{2 \sum\left(x_{i}\right)\left[\sqrt{2} \sum\left(z_{i}\right)\right]}
$$

Standard error $\left(\frac{1}{\hat{N}_{T}}\right)=\sqrt{\frac{8\left(\bar{z}^{2} s_{x}^{2}+2 \bar{x} \bar{z} s_{x z}+\bar{x}^{2} s_{z}^{2}\right)}{n}}$
where $\quad \bar{x}=$ Mean value of point-to-organism distances
$\bar{z}=$ Mean value of T-square organism-to-neighbor distances

$n=$ Sample size
$s_{x}^{2}$. V Variance of point-to-organism distances
$s_{z}^{2}=$ variance of T-square organism-to-neighbor distances
$s_{x z}=$ covariance of $x$ and $z$ distances

## Distance methods

- Point quarter method
- Forestry
- Early land surveying



## Distance methods

- Point quarter method

$$
\hat{N}_{p}=\frac{4(4 n-1)}{\pi \sum\left(r_{i j}^{2}\right)}
$$


where $\quad \hat{N}_{p}=$ Point-quarter estimate of population density
$n=$ Number of random points
$\pi=3.14159$
$r_{i j}=$ Distance from random point $i$ to the nearest organism in quadrant $j(j=1,2,3,4 ; i=1, \ldots n)$

Variance $\left(\hat{N}_{p}\right)=\frac{\hat{N}_{p}^{2}}{4 n-2}$

## Mark Recapture methods

1. Capture and mark individuals

- Radio transmitters, PIT tags, ear tags, physical features, genetics, etc.

2. Recapture or resight random sample of individuals during subsequent surveys
3. Calculate the proportion of new and previously captured/ sighted individuals.

## Mark-Recapture Methods

Three Standard Methods

1. Petersen Method - closed population, single recapture event
2. Schnabel Method - closed population, multiple recapture events
3. Jolly-Seber Method - open population, multiple censusing events

- Closed population: doesn't change in size during study
- Open population: population changes in size


## Petersen Method

One mark and one recapture session

$M=$ Number of individuals marked during the first sample
$C=$ Total number of individuals captured during the second sample
$R=$ Number of individuals in the second sample that were marked
$N=$ Size of the population at the time of Marking.

## Petersen Method

- If the number of recaptures is less than $7(R<7)$, add the value of 1 to each of the number Marked, Captured and Recaptured

$$
\widehat{N}=\frac{(M+1)(C+1)}{(R+1)}-1
$$

## Petersen - Confidence Intervals

How you Calculate Confidence Intervals depends on number of Recaptures relative to Total Captures at second marking session.

- If the proportion of recaptured individuals is greater than $10 \%$ of the total captures on the second sampling period ( $R / C>0.1$ ), then use a Binomial Confidence Interval.
- If $R / C$ is less than $10 \%$, but the number of recaptures is greater than 50 ( $\mathrm{R}>50$ ), then use a Normal Approximation
- If $R / C$ is less than $10 \%$ and $R<50$, you use a Poisson Confidence Interval


## Petersen - Confidence Intervals

## Binomial Confidence Interval

- X-axis = Recaptures /Captures
- Lines -Captures
- Y-Axis - Upper and lower Confidence Intervals for a given $\mathrm{R} / \mathrm{C}$.

$$
\widehat{N}=\frac{C M}{R}
$$

Lower $95 \%$ CI on $\widehat{N}=\frac{1}{\text { Upper pop.proportion }} M$ Upper $95 \%$ CI on $\widehat{N}=\frac{1}{\text { Lower pop.proportion }} M$


## Petersen - Confidence Intervals

Binomial Confidence Interval

- M: 50 marked birds
- C: 22 captured birds
- R: 14 recaptures
- Sample prop. $p=R / C=14 / 22=0.60$
- Captures = 22
- Lower confidence value $=0.4$
- Upper confidence value $=0.83$
$-\quad \mathrm{CU}=(1 / \mathrm{CV}) * \mathrm{M}$
- Lower $95 \% \mathrm{Cl}=(1 / 0.4) * 50=60$
- Upper $95 \% \mathrm{Cl}=(1 / 0.83) * 50=125$



## Petersen - Confidence Intervals

## Poisson Confidence Interval

- X in table corresponds to number of
Recaptures in your sample (R)
- Sub upper and lower values into estimate of $\mathbf{N}$ for low recaptures to get upper and lower Cl

$$
\widehat{N}=\frac{(M+1)(C+1)}{(R+1)}-1
$$

TABLE 2.1 CONFIDENCE LIMITS FOR A POISSON FREQUENCY DISTRIBUTION. Given the number of organisms observed ( $x$ ), this table provides the upper and lower limits from the Poisson distribution. Do not use this table unless you are sure the observed counts are adequately described by a Poisson distribution.

| $x$ | 95\% |  | 99\% |  | $x$ | 95\% |  | 99\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | . Lower | Upper | Lower | Upper |  | Lower | Upper | Lower | Upper |
| 0 | 0 | 3.285 | 0 | 4.771 | 46 | 34.05 | 60.24 | 29.90 | 65.96 |
| 1 | 0.051 | 5.323 | 0.010 | 6.914 | 47 | 34.66 | 61.90 | 31.84 | 66.81 |
| 2 | 0.355 | 6.686 | 0.149 | 8.727 | 48 | 34.66 | 62.81 | 31.84 | 67.92 |
| 3 | 0.818 | 8.102 | 0.436 | 10.473 | 49 | 36.03 | 63.49 | 32.55 | 69.83 |
| 4 | 1.366 | 9.598 | 0.823 | 12.347 | 50 | 37.67 | 64.95 | 34.18 | 70.05 |
| 5 | 1.970 | 11.177 | 1.279 | 13.793 | 51 | 37.67 | 66.76 | 34.18 | 71.56 |
| 6 | 2.613 | 12.817 | 1.785 | 15.277 | 52 | 38.16 | 66.76 | 35.20 | 73.20 |
| 7 | 3.285 | 13.765 | 2.330 | 16.801 | 53 | 39.76 | 68.10 | 36.54 | 73.62 |
| 8 | 3.285 | 14.921 | 2.906 | 18.362 | 54 | 40.94 | 69.62 | 36.54 | 75.16 |
| 9 | 4.460 | 16.768 | 3.507 | 19.462 | 55 | 40.94 | 71.09 | 37.82 | 76.61 |
| 10 | 5.323 | 17.633 | 4.130 | 20.676 | 56 | 41.75 | 71.28 | 38.94 | 77.15 |
| 11 | 5.323 | 19.050 | 4.771 | 22.042 | 57 | 43.45 | 72.66 | 38.94 | 78.71 |
| 12 | 6.686 | 20.335 | 4.771 | 23.765 | 58 | 44.26 | 74.22 | 40.37 | 80.06 |
| 13 | 6.686 | 21.364 | 5.829 | 24.925 | 59 | 44.26 | 75.49 | 41.39 | 80.65 |
| 14 | 8.102 | 22.945 | 6.668 | 25.992 | 60 | 45.28 | 75.78 | 41.39 | 82.21 |
| 15 | 8.102 | 23.762 | 6.914 | 27.718 | 61 | 47.02 | 77.16 | 42.85 | 83.56 |
| 16 | 9.598 | 25.400 | 7.756 | 28.852 | 62 | 47.69 | 78.73 | 43.91 | 84.12 |
| 17 | 9.598 | 26.306 | 8.727 | 29.900 | 63 | 47.69 | 79.98 | 43.91 | 85.65 |
| 18 | 11.177 | 27.735 | 8.727 | 31.839 | 64 | 48.74 | 80.25 | 45.26 | 87.12 |
| 19 | 11.177 | 28.966 | 10.009 | 32.547 | 65 | 50.42 | 81.61 | 46.50 | 87.55 |
| 20 | 12.817 | 30.017 | 10.473 | 34.183 | 66 | 51.29 | 83.14 | 46.50 | 89.05 |
| 21 | 12.817 | 31.675 | 11.242 | 35.204 | 67 | 51.29 | 84.57 | 47.62 | 90.72 |
| 22 | 13.765 | 32.277 | 12.347 | 36.544 | 68 | 52.15 | 84.67 | 49.13 | 90.96 |
| 23 | 14.921 | 34.048 | 12.347 | 37.819 | 69 | 53.72 | 86.01 | 49.13 | 92.42 |
| 24 | 14.921 | 34.665 | 13.793 | 38.939 | 70 | 54.99 | 87.48 | 49.96 | 94.34 |
| 25 | 16.768 | 36.030 | 13.793 | 40.373 | 71 | 54.99 | 89.23 | 51.78 | 94.35 |
| 26 | 16.77 | 37.67 | 15.28 | 41.39 | 72 | 55.51 | 89.23 | 51.78 | 95.76 |

## Petersen - Confidence Intervals

TABLE 2.1 CONFIDENCE LIMITS FOR A POISSON FREQUENCY DISTRIBUTION. Given the number of organisms observed ( $x$ ), this table provides the upper and lower limits from the Poisson distribution. Do not use this table unless you are sure the observed counts are adequately described by a Poisson distribution.

## Poisson Confidence Interval

- M: 85 marked snakes
- C: 42 captured snakes
- R: 4 recaptures
- Lower confidence value $=1.366$
- Upper confidence value $=9.598$

$$
\widehat{N}=\frac{(M+1)(C+1)}{(R+1)}-1
$$

$$
\begin{aligned}
\mathrm{N} & =(85+1)(42+1) /(4+1)-1=739 \\
\text { Upper } 95 \% \mathrm{Cl} & =(85+1)(42+1) /(1.366+1)-1=1562 \\
\text { Lower } 95 \% \mathrm{Cl} & =(85+1)(42+1) /(9.598+1)-1=348
\end{aligned}
$$

## Petersen - Assumptions

## Assumptions of the Petersen Method

- The Population is closed, so that N is constant
- All animals have the same chance of getting caught in the first sample
- Marking individuals does not affect their catchability
- Animals do not lose marks between the two sampling periods
- All marks are reported upon discovery in the second sample



## Schnabel Method

## Extension of Petersen Method with multiple marking events

- Number of Marked individuals accumulate with each time interval.

$$
\widehat{N}=\frac{\sum_{t}\left(C_{t} M_{t}\right)}{\sum_{t} R_{t}}
$$

- $C_{t}=$ Total number of individuals caught in sample $t$
- $R_{t}=$ Number of individuals already marked when caught at sample $t$
- $U_{t}=$ Number of individuals marked for first time and released in sample $t$
- $M_{t}=$ The number of marked individuals in the population just before sample $t$ is taken. (essentially, the cumulative number of $U_{t}$ up to $t-1$ )

$$
-\quad \mathrm{M} 6=\mathrm{U} 1+\mathrm{U} 2+\mathrm{U} 3+\mathrm{U} 4+\mathrm{U} 5+\mathrm{U} 6
$$

## Schnabel - Confidence Intervals

If $\sum R_{t}<50$, use values from a Poisson table

If $\sum \boldsymbol{R}_{\boldsymbol{t}}>5$, calculate with a normal approximation

$$
\frac{1}{\hat{N}} \pm t_{\alpha} \text { S.E. }
$$

where S.E. $=$ standard error of $1 / \mathrm{N}$
$t_{\alpha}=$ value from Student's t-table for $(100-\alpha) \%$ confidence limits.

## Schnabel - Confidence Intervals

If $\sum R_{t}>50$, calculate with a normal approximation

$$
\frac{1}{\hat{N}} \pm t_{\alpha} \mathrm{S} . \mathrm{E} .
$$

where S.E. $=$ standard error of $1 / \mathrm{N}$
$t_{\alpha}=$ value from Student's t-table for (100- $\alpha$ ) \% confidence limits.

$$
\begin{gathered}
\text { Variance }\left(\frac{1}{\hat{N}}\right)=\frac{\sum R_{t}}{\left(\sum C_{t} M_{t}\right)^{2}} \\
\text { Standard error of }\left(\frac{1}{\hat{N}}\right)=\sqrt{\operatorname{Variance}\left(\frac{1}{\hat{N}}\right)}
\end{gathered}
$$

## Vital rates

- Fundamental parameter of population change: birth rates, death rates
- Birth rates: number of individuals born/individual
- Death rates: number of individuals die/individual
- Probability of survival $=1-\mathrm{P}$ (mortality)
- Why are population ecologists interested in vital rates?


## Vital rate estimation



Problems

- Sample size
- Feasibility of sampling
- Hidden behavior
- Intrinsic variability
- Time frame
- Difficulty collecting data describing vital rates


## Birth rates: Fecundity

- "number of female offspring produced per adult female per unit of time"
- Often generalized to the number of young produced per female per unit of time
- If interested in population productivity then must know the sex ratio of the young
- "Young" often constituted as:
- Number of zygotes
- Number of viable young
- Number of individuals recruited into next time step
- Natality is synonymous with birth rate
- Ratio of live births in area to population of area (births/1000 individuals/year)


## Measuring birth rates

- Direct methods
- Observe number of offspring at natal site
- Some mammal and birds (eggs, litter size)
- Link between adult and offspring (somewhat)
- Observe number of young at breeding site
- Weak or no link between adult and offspring
- Placental scars from managed mammal populations


## Measuring birth rates

- Indirect methods
- Evidence of offspring at different stages



Upstream spawning trap


Female weight Gonadal weight


Egg weight GSI estimate


Estimate fry per redd

